Indices on Cryptocurrencies: an Evaluation

Konstantin Häusler [*]
Hongyu Xia [*2]

[*] Humboldt-Universität zu Berlin, Germany
[*2] Xiamen University, China

International Research Training Group 1792

Indices on Cryptocurrencies: an Evaluation

Konstantin Häusler · Hongyu Xia

Abstract Several cryptocurrency (CC) indices track the dynamics of the rising CC sector, and soon ETFs will be issued on them. We conduct a qualitative and quantitative evaluation of the currently existing CC indices. As the CC sector is not yet consolidated, index issuers face the challenge of tracking the dynamics of a fast-growing sector that is under continuous transformation. We propose several criteria and various measures to compare the indices under review. Major differences between the indices lie in their weighting schemes, their coverage of CCs and the number of constituents, the level of transparency, and thus their accuracy in mapping the dynamics of the CC sector. Our analysis reveals that indices that adapt dynamically to this rising sector outperform their competitors. Interestingly, increasing the number of constituents does not automatically lead to a better fit of the CC sector. All codes are available on Quantlet.com

Keywords Cryptocurrency · Index · Market Dynamics · Bitcoin

Konstantin Häusler
IRTG 1792 "High Dimensional Non-Stationary Time Series"
Humbolt Universität zu Berlin
E-mail: konstantin.haeusler@hu-berlin.de

Hongyu Xia
Xiamen University
Wang Yanan Institute for Studies in Economics (WISE)

1 Introduction

Indices are widely used to track the market dynamics of financial sectors. Several research groups and companies developed indices for the rising cryptocurrency (CC) sector, each of them with different methodological approaches for tracking the highly volatile and dynamic CC market (cf. Härdle and Trimborn [2015] p.17, Rivin and Scevola [2018], Elendner [2018]). This paper aims to compare and evaluate the characteristics of the currently existing CC-Indices: Bloomberg Galaxy Crypto Index (BGCI), Bitwise 10 Large Cap Crypto Index (Bitwise 10), the CRIX, CCi30, F5 crypto index, HODL5, Nasdaq Crypto Index and Ultra Cap 5 index. Figure 1 displays the index values of the aforementioned indices, scaled to 1000 points during 15-08-2018 to 28-02-2021.
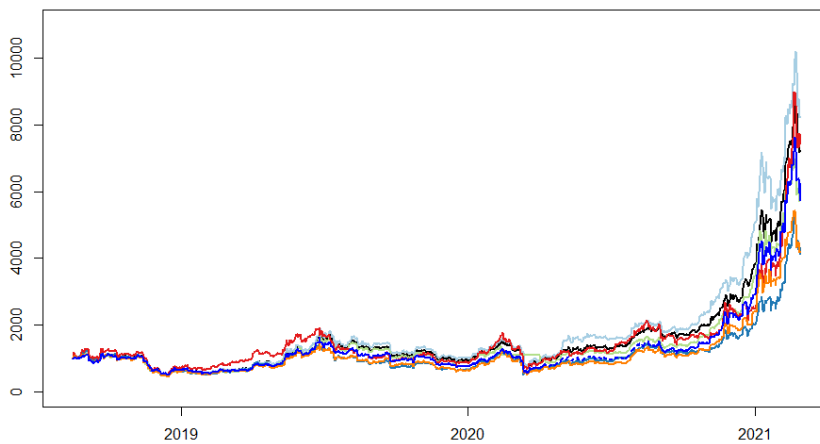

Fig. 1: Scaled CC indices: BBGCI, Bitwise 10, CCi30, CRIX, F5, HODL5, and the total market index (TMI, black solid line). The indices deviate from the TMI due to methodological differences in their construction. ⌕ evaluation_indices

In this paper, we examine the indices both qualitatively and quantitatively. Starting with the qualitative analysis, we elaborate the methodological differences between the indices. There is no 'right' or 'wrong' in constructing an index, each approach has its raison d'être, but they yield by construction different index values with dissimilar properties. A complete index should contain all available CCs weighted by their market capitalization, though this is practically not feasible because of the high effort involved (trading costs, steady re-balancing, ...). Therefore, any index issuer must make some sim-

plifying assumptions that affect the properties of the respective index. These methodological differences are elaborated in Section 2.3. Ultimately, we group the indices into three groups based on their methodology: purely market cap weighted indices, adjusted market cap weighted indices and manually weighted indices.

The quantitative analysis follows in Section 3. Index values themselves cannot be interpreted meaningfully, therefore we suggest several comparison criteria: Firstly, accuracy in mapping the dynamics of the CC sector. We tackle this criteria by constructing a total market index (TMI), which consists of all available CCs weighted by market capitalization, and we compute the correlation of each index to the TMI. Additionally, we obtain confidence intervals for the correlations through bootstrapping. Secondly, we require the indices to have similar statistical characteristics as the TMI. Therefore, we analyze the moments of the return distributions (volatility, kurtosis, skewness) of each CC index, which are important indicators for financial decision makers and investors. Thirdly, based on these moments, we compute several measures, through which we compare the indices quantitatively. The first is the Probabilistic Sharpe Ratio (PSR), introduced by Bailey and Lopez de Prado [2012], which extends the confidence intervals of the well-known Sharpe Ratio by an Edgeworth expansion of higher moments. Thereby, we can assess the robustness and statistical significance of Sharpe Ratios. This approach is appropriate, since the returns of the CC sector are highly non-normal (cf. Zhang et al. [2018], Petukhina et al. [2021]). The second is the Maximum Drawdown (MMD), an asymmetric risk measure. The MMD is defined as the percentage loss from the local maximum to the local minimum of an index i during a fixed time period. We include this measure, because the CC sector is not yet consolidated and CCs are nowadays mostly used as speculative investment asset.

Our analysis reveals several insights: First, and most surprisingly, a broader coverage of CCs by an index does not automatically yield in a better mapping of the CC sector's dynamics. The best example is given by HODL5 (five constituents) and CCi30 (thirty constituents): both make adjustments to the market capitalization in their weighting schemes, but HODL5 outperforms CCi30 in terms of accuracy (correlation with TMI) and PSR. The argument by Rivin and Scevola [2018], an increasing number of constituents yields in more diversification, seems to have been invalidated. This is not surprising, since Keilbar and Zhang [2021] identified several cointegration relationships among the top CCs and Zhang et al. [2018] report correlations among the returns of many CCs, especially to Bitcoin. Second, purely market cap weighted indices perform well. Adjustments in the weighting schemes are not very beneficial. Bitwise 10 and the CRIX, the only purely market cap weighted indices under review, yield very high returns, and their Sharpe Ratios are the highest among the CC indices. Introducing a cap/floor to some constituents (cf. BGCI, HODL5) does not only distort the mapping of the CC sector's dynamics, it also affects the statistical properties of indices negatively (i.e. SR, PSR,

MMD). From a methodological point of view, we consider the purely market cap weighting approach as the "correct" one, as it maps the CC sector's dynamics accurately. In practice, this approach is widely employed in classical financial sectors, as indices like the S&P 500 or the German DAX are constructed in such a way.

Third, transparency. The CC sector is not yet consolidated and the underlying technological mechanisms are not understood by the public (Härdle et al. [2020]. As for any currency, trust is crucial for the acceptance of CCs. The CC indices could promote trust through transparency, e.g. by disclosing the construction mechanisms, weighting schemes and index data. Unfortunately, this is not the case for all the indices under review. We do not know which index will emerge as the leading benchmark for the CC sector, but transparency will certainly be a factor.

The only index that satisfies all criteria is the CRIX. It is a purely market cap weighted index, its methodological approach is well-grounded (cf. Härdle and Trimborn [2015], Trimborn and Härdle [2018]), its index data is publicly available (on thecrix.de), it closely tracks the market dynamics (cf. Figure 4) and by its iterative algorithm, it optimally benefits from the gains of the rise of the CC sector (cf. Table 2). As the CC sector is under continuous transition and not yet consolidated (cf. Figure 3), the CRIX as the only index with dynamic adaption to the sector outperforms its competitors.

The remainder of this paper is structured as follows: Section 2 explains the particularities of the CC sector and introduces the CC indices under review. Section 3 conducts the quantitative comparison of the indices by several measures. Section 4 discusses the pros & cons of the indices. All codes are available on evaluation_indices

2 Data

2.1 The CC sector

As the CC sector is rising, the market capitalization of this sector is steadily growing. By the end of 2020, the overall market cap of the CC sector exceeded $743 Billion, which is roughly equivalent to Switzerland's gross domestic product. Figure 2 displays the market capitalization of i) the overall CC sector (black line), ii) the Top 10 CCs (by market cap, blue line), iii) the Top 30 CCs (red line) and iv) Bitcoin (green line). The parallel movement of the time series supports the finding of Keilbar and Zhang [2021], who revealed cointegration relationships among the top CCs. The decoupling of the entire CC sector from Bitcoin suggests that a new altcoin season could occur in 2021.

Simultaneously to the growth of the market capitalization, the number of CCs is growing. The increased attention in 2017/2018 yielded in the evolu-
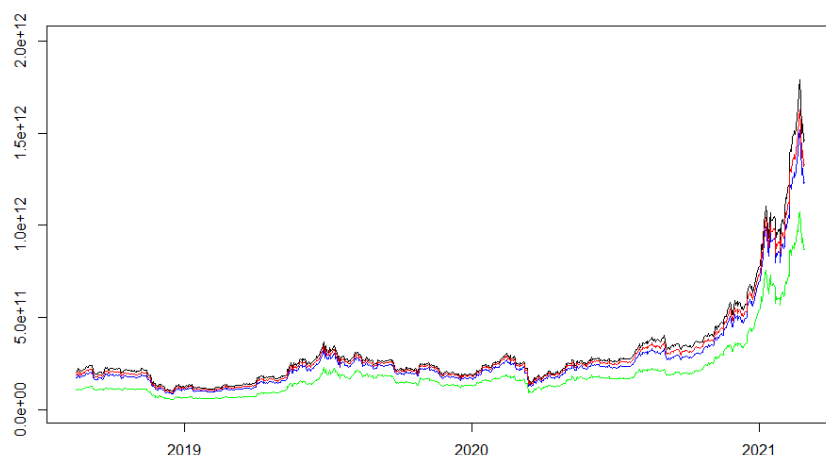
Fig. 2: Market Capitalization of the overall CC sector (black line), the Top 10 (blue) & Top 30 (red) CCs by market capitalization and Bitcoin (green). Data source: coingecko.com. **Q** evaluation_indices

tion of new CCs, and throughout 2019 it seemed that the CC sector consolidated. This phase also includes Paypal's announcement of Bitcoin as a payment method. In mid-2020 though, the creation of new CCs continued, whether this is driven by the economic turmoil caused by the Covid pandemic or the increased acceptance and applications of CCs (Hou et al. [2020], Härdle et al. [2020]) remains to be seen.

Besides the growth of the market capitalization and the increasing number of CCs, it is worth noting that the composition of the top 10 and top 30 CCs (by market capitalization) is under constant transformation. Figure 3 displays the composition and share of the top 10 CCs for the period of 2018-01 to 2021-06. Each bar refers to the market share of the top 10 CCs at the first day of each quarter, each colour indicates the share of the respective CC. Some insights are directly observable: the share of Bitcoin changes continuously, in January 2018 Bitcoin represented 38% of the CC sector, though in October 2019 its share reflected 67%. Furthermore, the top 10 CCs represent between 80 − 90% of the overall CC sector, depending on the time point. But most importantly, only within the three years under review, the composition of the top 10 CCs changed very often; only Bitcoin, Bitcoin-Cash, Ethereum and Ripple were at each stage present in the top 10. In total, 20 CCs appeared in the top 10 in recent years. Mapping these dynamics poses major challenges to index issuers.
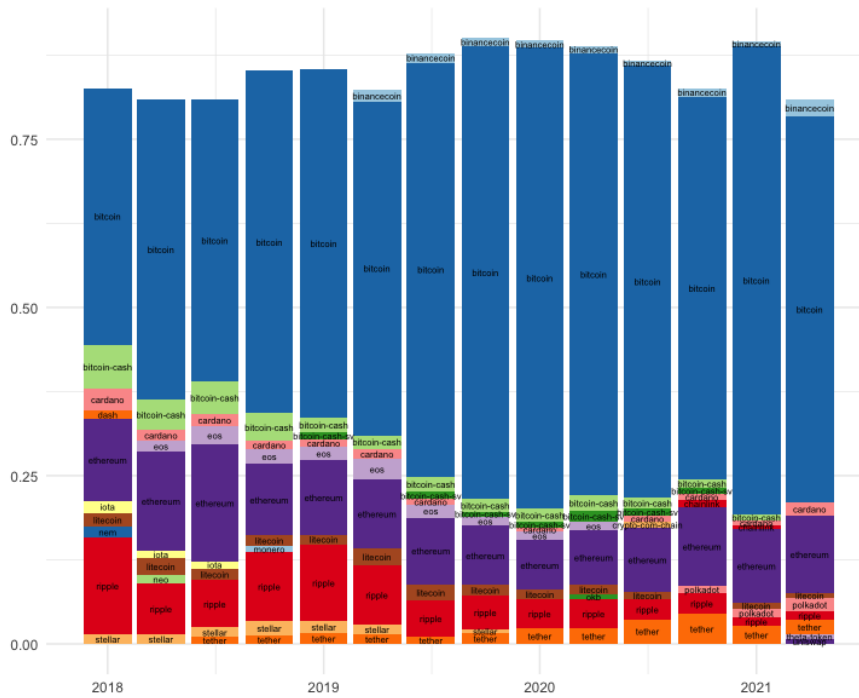
Fig. 3: Share of the top 10 CCs by market cap, over time (quarterly, 2018-01 to 2021-06). ⌕ evaluation_indices

2.2 CC data and Index data

Two data sets are used in the analysis: daily data of all publicly traded CCs is obtained from coingecko.com. The authors thankfully acknowledge their freely accessible API that allows retrieving information on prices, volumes and market capitalization for each CC. In addition, data on CC indices is thankfully provided by Bloomberg, f5 crypto capital, CCi30 and thecrix.de. As the CC market is not centrally organized, no central authority issues an industry benchmark index. The aforementioned index issuers and data providers are partially research units and partially private companies. Their methodological approaches differ significantly, which is the topic of the following paragraphs. The period of the analysis is restricted to August 2018 to February 2021. The reasoning is rather practically than theoretically founded, because many of the indices have been just recently issued and their historical values are thus not available.

2.3 Compositon of Indices

Bitwise 10 Bitwise 10 Large Cap Crypto Index is a CC index by San Francisco-based company Bitwise Asset Management. Their CC index covers the ten biggest CCs by market capitalization, not including stablecoins (=CCs that are pegged to a fiat currency). The index is constructed by weighting each constituent by the free-float and inflation adjusted market capitalization. Unfortunately, the exact weighting scheme is not known to the authors. Bitwise's other indices, Bitwise 20, Bitwise 70, Bitwise 100, are constructed in a similar manner. Most recently, Bitwise issues an index fund based on Bitwise 10.

BGCI Bloomberg Galaxy Crypto Index is issued by Bloomberg in cooperation with Galaxy Crypto. The index consists of at most 12 constituents, which are the biggest CCs ranked by market capitalization. The contribution of each constituent to the final index is capped at 40% and floored by 1%. Unfortunately, Bloomberg does not publish its guidelines on which base they determine the number of constituents of its index. The index values are calculated by

$$BGCI_t = \frac{\sum_{i=1} P_{i,t} \times Q_{i,m} \times CF_{i,m}}{D}$$

where $P_{i,t}$ is the price of constituent i at time t, $Q_{i,m}$ the circulating supply of each constituent i in month m and $CF_{i,m}$ the cap/ floor correction factor; D is a divisor for scaling. If a constituent exceeds the cap, its remaining weight is redistributed among the other constituents relative to their market capitalization.

CRIX The CRyptocurrency IndeX has been developed at the Blockchain Research Center at Humboldt University Berlin by Härdle and Trimborn [2015] and is constructed as a Laspeyres index that weights the market capitalization of its constituents relative to the base year 2015.

$$CRIX_t = \frac{\sum_i P_{it} Q_{i0}}{\sum_i P_{i0} Q_{i0}}$$

where P_{it} refers to the price of CC i at time t and Q_{it} to the amount of CC i. The number of included coins is adjusted dynamically, to ensure that the CRIX represents the total CC sector accurately. The selection of the constituents is done by an iterative algorithm that penalizes for an increasing number of constituents but aims to minimize the deviance of the portfolio to the total CC market. As selection criterion, the AIC is applied to balance the CRIX between a sparse number of constituents and an accurate representation of the whole CC market. Furthermore, only liquid CCs are eligible to be included on the index.

CCi30 Cryptocurrency Index 30 selects the top 30 CCs by adjusted market capitalization, excluding stablecoins. The index, developed by Rivin and Scevola [2018] is fully transparent and replicable, and historical index values are available on cci30.com.

The weight of each constituent to the index is computed by the square root of its adjusted market capitalization relative to the adjusted market capitalization of the other constituents. The adjusted market capitalization itself is smoothed exponentially to represent a moving average over past periods and to remove temporary fluctuations. Formally, the index values are calculated by

$$CCi30_t = \sum_{j=1}^{30} \frac{\sqrt{M_j^*(t)}}{\sum_{i=1}^{30} \sqrt{M_i^*(t)}} \frac{P_j(t)}{P_j(0)}.$$

where P_j is the price of constituent j and the adjusted market capitalization M^* is weighted in the following way:

$$M^*(t) = \frac{\sum_{i=0}^{\infty} M(T-i)e^{-\alpha i}}{\sum_{i=0}^{\infty} e^{-\alpha i}}$$

Rivin and Scevola [2018] argue that the dominance of Bitcoin and Ethereum is reduced by taking the square root of the adjusted market capitalization of each coin. Following their argumentation, smaller CCs beyond Bitcoin & Ethereum get thereby more weight and the index is more diversified.

F5 The F5 crypto index issued by Berlin-based start-up F5 Crypto Capital (cf. Elendner [2018]) is a CC index which consists of the 12 biggest CCs by market capitalization. Excluded are stablecoins, anonymous CCs and CCs that are traded less than 100 days. The weights of each constituent to the F5 index is computed by its *momentum*:

$$momentum_t = price_t - price_{t-n}$$

The weight allocation by the momentum strategy already reveals the purpose of the index as an investment tool: the best performing CCs get more weight. Jegadeesh and Titman [1993] have shown that the *momentum* strategy works for stock markets, however it still lacks a theoretical foundation. The quantitative analysis in Section 3 will elaborate whether the *momentum* strategy also succeeds in the CC sector.

HODL5 The CC index HODL5 is issued by Amun Technologies Limited, and aims to track the performance of the top 5 most liquid CCs. Interestingly, CCs are not selected according to their current market capitalization, but according to their projected market capitalization in 2050. The index is constructed using the Laspeyres' form:

$$HODL5_t = \frac{\sum_{i=1} P_{t,i} * Q_{t,i} * CF_{t,i}}{D_t}$$

where $P_{t,i}$ refers to the price of CC i, $Q_{t,i}$ is amount of CC i outstanding, $CF_{t,i}$ is weighting cap/floor correction factor, and D_t is the stability and scaling divisor. The cap/floor correction factor is imposed to guarantee diversification and avoid under- and over-weighting.

NCI The Nasdaq Crypto Index is developed by Nasdaq, Inc. and the crypto asset manager Hashdex and they offer the corresponding Hashdex ETF available on Bermuda Stock Exchange (BSX). It's asset eligibility principles is about core exchanges, core custodians, free-floating trading volume and price. The index values are calculated by:

$$NCI_t = \frac{\sum_i^C Q_{t,i} P_{t,i}}{D_t}$$

where $Q_{t,i}$ is the supply of CC i fixed on the previous reconstitution and rebalance date. The divisor D_t is used for scaling and smooth transitions at the rebalancing dates. The set of constituents C is not precisely defined. NCI is not included in the quantitative analysis of Section 3, because historical values are not available, since the index was just issued recently.

UC5 The CF Cryptocurrency Ultra Cap 5 Index is issued by CF Benchmarks Ltd. It aims to track the performance of the top 5 largest CCs by market capitalization, excluding stablecoins, and aims to be used as a bennchmark for the CC sector as defined by the EU Bennchmark Regulations ("EU BMR"). It is caluclated as follows:

$$UC5_t = \frac{\sum_i a_{i,t} Q_{i,t} P_{i,t}}{D_i}$$

where a_i is the free float adjustment factor, $P_{i,t}$ is the price of constituent i at time t, and D is the scaling and smoothing divisor. The Ultra Cap weights its constituents by free float market capitalization. Its historical data is not available.

Table 1: Composition of CC Indices

Index	# of Constituents	Index & Weights	Abbreviations
BGCI	≤12	$BGCI_t = \frac{\sum_i P_{i,t} \times Q_{i,m} \times CF_{i,m}}{D}$	$Q_{i,m}$ = circulating supply of each constituent i at month m $CF_{i,m}$ = Cap/Floor correction factor: max weight at 40%, min weight 1%.
Bitwise 10	10	weighted market cap	
CCi30	30	$CCi30_t = \sum_{j=1}^{30} \frac{\sqrt{M_j^*(t)}}{\sum_{i=1}^{30} \sqrt{M_i^*(t)}} \frac{P_j(t)}{P_j(0)}$	M^* = moving-average adjusted Market Cap of CC j
CRIX	dynamic adjustment due to AIC	$CRIX_t = \frac{\sum_i P_{it} Q_{i0}}{\sum_i P_{i0} Q_{i0}}$	P_{it} = price of CC i at time t Q_{it} = supply of CC i at time t
F5	12	manually weighted by their momentum	$momentum_t = price_t - price_{t-n}$
HODL5	5	$HODL5 = \frac{\sum_i P_{t,i} Q_{t,i} CF_{t,i}}{D_t}$.	CF_i=Cap/Floor correction factor (if applicable, otherwise set to 1)
NCI	Unset	$NCI_t = \frac{\sum_i Q_{i,t} P_{t,i}}{D}$	$Q_{i,t}$ = supply of asset i fixed on the previous rebalance date
UC5	5	$UC5_t = \frac{\sum_i a_{i,t} Q_{i,t} P_{i,t}}{D_i}$	a_i free float supply adjustment

2.4 Classification of Indices

A tabular comparison of the index methodologies is summarized in Table 1. The main differences between the approaches concern the number of constituents and their weighting scheme to the respective index. We categorize the CC indices based on their methodological approaches in three categories: First, market cap weighted indices. This group comprises Bitwise 10, the CRIX, NCI and Ultra Cap 5. Second, adjusted market cap indices. This group comprises BGCI, CCi30 and HODL5. Third, manually weighted indices. This group consists of F5.

The first group, market cap weighted indices, are constructed as Laspeyre indices and constituents are weighted by their market cap. The striking difference between them refers to the selection of constituents: UC5 takes the top 5 CCs by market cap, Bitwise 10 the top 10, whereas the CRIX selects dynamically the optimal number of constituents by some AIC/BIC information criteria. The number of constituents of the NCI varies as well.

The second group, adjusted market cap indices, impose restrictions on the market cap weighting. This group is as well rather heterogeneous: the number

of constituents varies from 5 (HOLD5)to 30 (CCi30). All of them make adjustments to the market caps: the general reasoning is to break the dominance of Bitcoin and Ethereum by limiting their weights (CCi30, BGCI, HODL5), and thus to allow for more diversification.

The third group, manually weighted indices, consists only of the F5 crypto index. The implementation of the *momentum* strategy by F5 followed the logic of stock markets (cf. Jegadeesh and Titman [1993], Carhart [1997], Jegadeesh and Titman [2001]), and its success (relatively high mean return) indicates that it works as well for the CC sector. The *momentum* strategy however is a purely empirical argument, and it is lacking theoretical foundation.

Some notes on the indices: the methodological approach of the indices is very different. The coverage of CCs varies a lot, from 5 (UC5 & HODL5) to 30 (CCi30). This opens the question whether an increasing number of constituents yields in a better mapping of the overall sector. Furthermore, it remains to be seen whether the adjustments to the market caps (group 2) impact the empirical properties (see Section 3), and whether these adjustments are beneficial. On the one hand side, the adjustments lead to more diversification among the constituents, but at the same time it may distort the mapping of the CC sector. Finally, the level of transparency of the indices varies a lot: some index issuers even publish their source code, others remain mysterious with regard to their mechanisms (choice of constituents, weighting algorithms) and the respective index values. As trust is crucial for financial sectors, we are curious to see which index outperforms its competitors.

3 Quantitative Evaluation of CC Indices

The objective of issuing an index can either be to track a market segment as accurately as possible or to construct an investment instrument on it that allows to diversify coin-specific risks and to benefit from overall market gains. Irrespective of the motivation, several comparison criteria are proposed to measure the performance of the CC Indices under review with regard to both motives.

Firstly, tackling the issue of accuracy, the correlation of each index to the scaled total market index (TMI) is taken as comparison criteria. This benchmark TMI is composed of all available CCs, weighted by their market capitalization and scaled to 1000 points as starting value. Such a TMI is an ideal theoretical construct, however, it is not feasible to implement it in practice since there are minimum trading amounts and trading fees.

As can be seen in Figure 4, all CC indices are highly correlated to the TMI. Each violinplot is obtained by bootstrapping: 1000 samples of 100 observations are taken from the data, for each sample the correlation between each index and the TMI is computed. The highest correlation reveal the CRIX, Bitwise 10 and HODL5. Direct inference from Figure 4 contains some pitfalls: the TMI
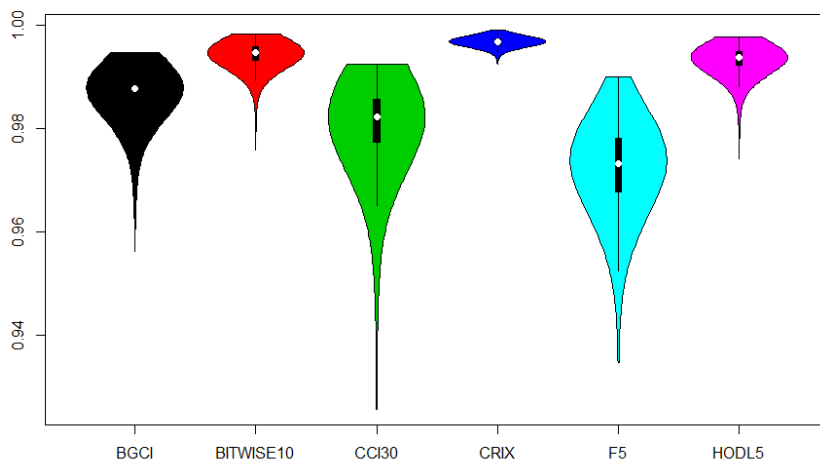
Fig. 4: Violinplots of the correlation between each index and the TMI. Densities obtained through bootstrapping. 🔍 evaluation_indices

itself is constructed as a market cap weighted index (cf. group 1 of Section 2.4). The high correlation of TMI with Bitwise 10 and the CRIX are partially caused by the same way of construction.

It is not surprising that all the indices are highly correlated to the TMI, however, it is surprising that HODL 5 is higher correlated with the TMI than CCi30 and BGCI. These three indices all belong to the second adjusted market cap group. The CCi30 and BGCI consist of 30 and up to 12 constituents respectively, HODL consists only of 5. This finding indicates that it is enough to track the top coins by market capitalization and to discard the rest. Hu et al. [2019] found similar results, their study showed that the returns of CCs are highly correlated, especially to the returns of Bitcoin. Additionally, Keilbar and Zhang [2021] identified multiple cointegration relationships among the top CCs, which supports the hypothesis that is enough to track a few top coins and to discard the rest.

Secondly, as the statistical properties of each index differ due to methodological differences of their composition, an analysis of their statistical properties is conducted, with a special focus on their moments. As comparison criteria, the Probabilistic Sharpe Ratio (PSR) introduced by Bailey and Lopez de Prado [2012] and the Maximum Drawdown (MMD) are used as performance measures. A normal Sharpe Ratio as a measure of return to risk is a point estimate constructed on empirical estimates based on historical values. In set-

tings where returns are non-normal, the classical Sharpe Ratio is not reliable, because higher moments have an impact on the confidence intervals of the estimated Sharpe Ratios, and thus on their statistical significance. The PSR instead corrects the confidence intervals for the non-normal higher moments.

As outlined by Lo [2002], the estimated variance of a Sharpe Ratio under the assumption that returns are normally distributed is given by

$$\hat{\sigma}(\widehat{SR}) = \sqrt{\frac{1}{n}\left(1 + \frac{1}{2}\widehat{SR}^2\right)} \tag{1}$$

However, in the overall CC market, returns are highly non-normal. As shown in Table 2, the properties of all indices differ from the normal distribution. Mertens [2002] suggests to adjust the confidence bands of Sharpe Ratios that are estimated based on non-normally distributed returns by higher moments. Loosening the assumption of normal returns (cf. Bailey and Lopez de Prado [2012]), the estimated variance of the Sharpe Ratio extends to

$$\hat{\sigma}(\widehat{SR}) = \sqrt{\frac{1}{n-1}\left(1 + \frac{1}{2}\widehat{SR}^2 - \gamma_3\widehat{SR} + \frac{\gamma_4 - 3}{4}\widehat{SR}^2\right)} \tag{2}$$

where γ_3 is the skewness and γ_4 the kurtosis. It is basically an Edgeworth expansion that adjusts for the non-normal higher moments. The PSR by Bailey and Lopez de Prado [2012] applies this standard deviation to assess the significance of the estimated Sharpe Ratios. Given a predefined benchmark SR^*, the PSR of Bailey and Lopez de Prado [2012] is defined as

$$PSR(SR^*) = \text{Prob}[SR^* \leq \widehat{SR}] \tag{3}$$

which can be estimated by

$$\widehat{PSR}(SR^*) = Z\left[\frac{\left(\widehat{SR} - SR^*\right)}{\hat{\sigma}(\widehat{SR})}\right] = Z\left[\frac{\left(\widehat{SR} - SR^*\right)\sqrt{n-1}}{\sqrt{1 + \frac{1}{2}\widehat{SR}^2 - \gamma_3\widehat{SR} + \frac{\gamma-3}{4}\widehat{SR}^2}}\right] \tag{4}$$

where Z refers to the cdf of the standard normal distribution.

Additionally, we propose the Maximum Drawdown (MMD) as comparison criteria. The MMD measures the peak-to-trough decline of a financial asset i during a fixed period (Magdon-Ismail and Atiya [2004], Ankenbrand and Bieri [2018]). As an asymmetric risk measure, it helps portfolio managers to make investment decisions. It is usually defined as the percentage loss of the peak value:

$$MMD_{i,t} = \frac{M_t - m_t}{M_t} * 100\% \tag{5}$$

where $M_{i,t} = max_{\mu \in [0,t]} P_{i,\mu}$, is the price peak of asset i during time period of $[0, t]$. $m_{i,t} = min_{\mu \in [0,t]} P_{i,\mu}$, is the price though of an asset during this time period.

	Group	returns %	sd	skewness	kurtosis	SR	PSR	MMD
TMI		0.287	0.038	-0.969	14.856	0.076	0.987	0.616
BITWISE10	1	0.249	0.034	-0.767	11.118	0.074	0.985	0.588
CRIX	1	0.304	0.039	-0.650	13.875	0.079	0.990	0.607
BGCI	2	0.241	0.042	0.047	8.986	0.058	0.961	0.674
CCI30	2	0.240	0.041	-0.931	13.418	0.059	0.958	0.639
HODL5	2	0.243	0.038	-0.187	6.871	0.065	0.974	0.648
F5	3	0.324	0.046	-0.660	11.145	0.071	0.982	0.652

Table 2: Descriptive Statistics on daily level for the CC indices under review, rounded values. Period of analysis 08/2018-06/2021. Abbreviations: sd- standard deviation of returns, SR - Sharpe Ratio, PSR - Probabilistic Sharpe Ratio, MMD - maximum drawdown. PSR given the benchmark $SR^* = 0$ (probability of positive Sharpe Ratios). Q evaluation_indices

Descriptive statistics for all indices whose historical data is available are summarized in Table 2. Unfortunately, we were not able to obtain data of the NCI and UC5. The column `returns` refers to daily returns, not annualized returns. Column `sd` displays the standard deviation of daily returns, `skewness` and `kurtosis` refer to the higher moments of the return distribution. The Sharpe Ratios (`SR`) assume a risk-free interest rate $r^* = 0$. Up to our knowledge, there is still no theoretical founded guideline which interest rate to choose for the computation of Sharpe Ratios in the context of CCs. The Probabilistic Sharpe Ratios `PSR` compare the Sharpe Ratios relative to the benchmark of $SR^* = 0$, see Equation 3. The values in `PSR` thus refer to the probability of positive Sharpe Ratio estimates. Finally, the column `MMD` is the Maximum Drawdown as defined in Equation 5.

The estimated returns seem quite low, but one has to consider that these are daily returns. Take TMI as an example, when transforming the daily return to yearly return by compound interest method, the mean yearly return is about 184.64%. Skewness and kurtosis differ for all indices by far from the normal distribution ($\gamma_3 \neq 0$, $\gamma_4 \neq 3$). Our estimates support the findings of Zhang et al. [2018] and Härdle et al. [2020] who report heavy tails of return distributions for many CCs. The non-normality of returns supports the application of the PSR.

Interestingly, the F5 crypto index and CRIX reveal the highest returns, 0.324% and 0.304%, respectively. In this regard, the CRIX comes closest to the TMI, which is not surprising as the iterative construction algorithm of the CRIX aims to minimize the deviance of the CRIX CC basket to the TMI.

Furthermore, the high return of the F5 index indicates that the *momentum* strategy (Jegadeesh and Titman [1993], Elendner [2018]) is effective in the CC market.

The highest Sharpe Ratios are achieved by the CRIX (0.079), Bitwise 10 (0.074) and F5 (0.071) . Interestingly, this corresponds to two members of Group 1 and Group 3 (cf. Section 2.4) . These estimates alone are not very informative, as the return distributions are highly non-normal. The PSR is a useful remedy to work around this issue. Given the benchmark $SR^* = 0$, we can interpret the PSR as the probability of obtaining positive Sharpe Ratios. Here we observe similar patterns: the highest PSR is achieved by the CRIX (0.990), followed by Bitwise 10 (0.985) and F5 (0.982), though the estimated PSRs are quite similar for all indices (due to the overall bullish market dynamics during the period of analysis).

The maximum drawdown, column `MMD`, measures the maximum percentage peak-to-trough decline of each index and the TMI. The total market's max drawdown is about 61.6%, the inglorious highest MMD is achieved by BGCI. The CRIX has the closest MMD value relative to the TMI.

The moments and measures of some CC indices (CCi30, CRIX) are closer to the TMI than others. This is partially due to the weighting schemes as described in Section 2.3 and partially by the coverage of CCs included. Others however (BGCI, HODL5, both Group 2), are closer to the normal distribution.

So which index performs best? The answer depends on the intentions of the questioner, regulators may prefer most accurate and transparent indices, investors the most profitable ones. That's the topic of the following section, which discusses the (dis-)advantages of the CC indices.

4 Discussion of CC Indices

An index that consists of all CCs would perfectly represent the dynamics of the CC sector. However, this is in practice not feasible due to the high effort involved (steady re-balancing, trading costs, minimum trading amounts, ...). Therefore, each issuer of an index must make simplifying assumptions, the details are outlined in Section 2.3. Consequently, these assumptions affect the statistical properties of the indices, which was the topic of the previous Section 3. But which index is now preferable? In this section, we discuss the advantages and disadvantages of the CC indices, how they approach the challenge of mapping the dynamics of a continuously transforming and rising sector as described in Section 2.1, and how accurate, robust and transparent they are.

Bitwise 10 The index scores with high accuracy in mapping the CC dynamics and a broad coverage of CCs. From an investor's point of view, the index seems

preferable due to its low MMD and high PSR. Interestingly, the plane market cap weighting scheme outperformed the adjustments of Group 2. Only a few minor flaws tarnish the picture: the exact weighting scheme is not disclosed and the trading costs can be considerable, as the top 10 CCs by market cap are under constant transformation (cf. Figure 3)

BGCI The analysis revealed some shortcomings in the construction and properties of the BGCI index. The cap/floor correction factor does reduce the dominance of Bitcoin, though it distorts the mapping of the CC sector's dynamics slightly. Furthermore, it is not quite clear how the number of constituents is determined. The resulting low (P)SR and high MMD are the consequences.

CCi30 Covering the top 30 CCs by market capitalization yields in high diversification and reduces the inherent risks of specific CCs. The disclosure of their methodological approach and the freely accessible index data promote transparency and thereby trust. However, there are two major downsides of this approach: firstly, the square-root adjustments to the market capitalization of each index distort the mapping of the CC sector dynamics. Secondly, the extensive list of covered CCs bears relatively high trading costs at each re-balancing date (though trading costs are relatively low in the CC sector).

CRIX The CRIX is characterized by many positive features: the dynamic adjustment through its iterative algorithm yields in an optimal mapping of the CC dynamics at low costs (i.e. a sparse number of constituents). In addition, this algorithm allows to benefit very closely from the gains of this rising sector, which is empirically supported by the high PSR and the high correlation to the TMI. A major downside lies in the relatively high transaction costs that occur due to the dynamic re-balancing and the in/exclusion of constituents.

F5 The only manually weighted CC index in this analysis performed well. Our prior beliefs that the returns generated by the *momentum* (cf. Elendner [2018]) strategy would be significantly different from the other indices turns out to be validated: the high returns and (P)SR indicate the the *momentum* strategy works as well for the CC sector. The downside of the *momentum* strategy however is its lack of theoretical foundation. Additionally, the undisclosed manual weighting does not promote transparency.

HODL5 Among the indices with adjustments in their weighting schemes (Group 2), HODL5 reveals high accuracy in mapping the CC dynamics. That is impressive, since the cap/floor correction factor distorts the mapping. However, the index's key figures are rather mediocre.

Overall, the indices deal in different ways with the challenge of mapping the dynamics of the rising CC sector. Our analysis reveals several insights: First, an increasing number of constituents covered by an index does not automatically yield in a better mapping of the CC sector's dynamics. The best example is given by HODL5 (five constituents) and CCi30 (thirty constituents): both make adjustments to the market capitalization in their weighting schemes, but HODL5 outperforms CCi30 in terms of accuracy. The argument by Rivin and Scevola [2018], an increasing number of constituents leads to more diversification, seems to have been invalidated. This is not surprising, since Keilbar and Zhang [2021] identified several cointegration relationships among the top CCs and Zhang et al. [2018] report correlations among the returns of many CCs, especially to Bitcoin.

Second, purely market cap weighted indices perform well. Adjustments in the weighting schemes are not very beneficial. Bitwise 10 and the CRIX yield very high returns, and their PSRs are among the highest of the indices under review. Introducing a cap/floor to some constituents (cf. BGCI, HODL5) does not only distort the mapping of the CC sector's dynamics, it also affects the statistical properties of indices negatively (i.e. SR, PSR, MMD). From a methodological point of view, we consider the purely market cap weighting approach as the "correct" one, as it maps the CC sector's dynamics accurately. In practice, this approach is widely employed in classical financial sectors, as indices like the S&P 500 or the German DAX are constructed in such a way. Third, transparency. The CC sector is not yet consolidated and the underlying technological mechanisms are not understood by the public (Härdle et al. [2020]. As for any currency, trust is crucial for the acceptance of CCs. The CC indices could promote trust through transparency, e.g. by disclosing the construction mechanisms, weighting schemes and index data. Unfortunately, this is not the case for all the indices under review. We do not know which index will emerge as the leading benchmark for the CC sector, but transparency will certainly be a factor.

The only index that satisfies all criteria is the CRIX. It is a purely market cap weighted index, its methodological approach is well-grounded (cf. Trimborn and Härdle [2018]), its index data is publicly available (on thecrix.de), it closely tracks the market dynamics (cf. Figure 4) and by its iterative algorithm, it benefits optimally from the gains of the rise of the CC sector (cf. Table 2). As the CC sector is under continuous transition and not yet consolidated (cf. Figure 3), the CRIX as the only index with dynamic adaption to the market outperforms its competitors.

5 Conclusion

The present paper examined the quantitative and qualitative properties of the currently existing CC indices. A detailed assessment of their composition, methodological differences, statistical properties and accuracy in represent-

ing the CC sector yielded several insights: First, the major differences in the construction of the indices lie in the weighting scheme and the number of constituents in each index. Surprisingly, a larger number of CCs included in an index does not necessarily lead to higher accuracy in the representation of the CC market. Second, purely market cap weighted indices perform well. Adjustments in the weighting schemes are not very beneficial. Bitwise 10 and the CRIX yield very high returns, and their PSRs are among the highest of the indices under review. Introducing a cap/floor to some constituents (cf. BGCI, HODL5) does not only distort the mapping of the CC sector's dynamics, it also affects the statistical properties of indices negatively (i.e. SR, PSR, MMD). We wonder which index will take the dominant position in this sector and act as a benchmark index. In our point of view, the CRIX developed by Trimborn and Härdle [2018] is the most suitable index due to its i) scientific foundation, ii) transparency and publicly available index data, and iii) its optimal solution to the fundamental trade-off every index is facing (a sparse number of constituents and high accuracy in mapping the CC sector's dynamics).

References

T. Ankenbrand and D. Bieri. Assessment of cryptocurrencies as an asset class by their characteristics. *Investment management and financial innovations*, (15, Iss. 3):169–181, 2018.

D. H. Bailey and M. Lopez de Prado. The sharpe ratio efficient frontier. *Journal of Risk*, 15(2):13, 2012.

M. M. Carhart. On persistence in mutual fund performance. *The Journal of finance*, 52(1):57–82, 1997.

H. Elendner. F5: optimised crypto-currency investment strategies. 2018.

W. K. Härdle and S. Trimborn. Crix or evaluating blockchain based currencies. *Oberwolfach Reports*, (42), 2015. doi: 10.4171/OWR/2015/42.

W. K. Härdle, C. R. Harvey, and R. C. Reule. Understanding cryptocurrencies. *Journal of Financial Econometrics*, 18:181–208, 2020.

A. J. Hou, W. Wang, C. Y. Chen, and W. K. Härdle. Pricing cryptocurrency options. *Journal of Financial Econometrics*, 18(2):250–279, 2020.

A. S. Hu, C. A. Parlour, and U. Rajan. Cryptocurrencies: Stylized facts on a new investible instrument. *Financial Management*, 48(4):1049–1068, 2019.

N. Jegadeesh and S. Titman. Returns to buying winners and selling losers: Implications for stock market efficiency. *The Journal of finance*, 48(1):65–91, 1993.

N. Jegadeesh and S. Titman. Profitability of momentum strategies: An evaluation of alternative explanations. *The Journal of finance*, 56(2):699–720, 2001.

G. Keilbar and Y. Zhang. On cointegration and cryptocurrency dynamics. *Digital Finance*, pages 1–23, 2021. doi: https://doi.org/10.1007/s42521-021-00027-5.

A. W. Lo. The statistics of sharpe ratios. *Financial analysts journal*, 58(4): 36–52, 2002.

M. Magdon-Ismail and A. F. Atiya. Maximum drawdown. *Risk Magazine*, 17 (10):99–102, 2004.

E. Mertens. Comments on variance of the iid estimator in lo (2002). Technical report, Technical report, Working Paper University of Basel . . . , 2002.

A. A. Petukhina, R. C. Reule, and W. K. Härdle. Rise of the machines? intraday high-frequency trading patterns of cryptocurrencies. *The European Journal of Finance*, 27(1-2):8–30, 2021.

I. Rivin and C. Scevola. The cci30 index. *arXiv preprint arXiv:1804.06711*, 2018.

S. Trimborn and W. K. Härdle. Crix an index for cryptocurrencies. *Journal of Empirical Finance*, 49:107–122, 2018.

W. Zhang, P. Wang, X. Li, and D. Shen. Some stylized facts of the cryptocurrency market. *Applied Economics*, 50(55):5950–5965, 2018.

IRTG 1792 Discussion Paper Series 2021

For a complete list of Discussion Papers published, please visit
http://irtg1792.hu-berlin.de.